# SYLLABUS

### Mathematical Analysis I (Differential calculus)

# 1. Data about the program of study

|     | Dutu usout the program of study |                                             |
|-----|---------------------------------|---------------------------------------------|
| 1.1 | Institution                     | Technical University of Cluj-Napoca         |
| 1.2 | Faculty                         | Automation and Computer Science             |
| 1.3 | Department                      | Mathematics                                 |
| 1.4 | Field of study                  | Systems Engineering                         |
| 1.5 | Cycle of study                  | Bachelor of Science                         |
| 1.6 | Program of study/Qualification  | Automation and Applied Informatics, English |
| 1.7 | Form of education               | Full time                                   |
| 1.8 | Subject code                    | 1.00                                        |
| 1.8 | Subject code                    | 1.00                                        |

# 2. Data about the subject

| 2.1 | Subject name    |        |        |            |                       | Mathematical Analysis I (Differential Calculus) |            |      |     |                  |       |
|-----|-----------------|--------|--------|------------|-----------------------|-------------------------------------------------|------------|------|-----|------------------|-------|
| 2.2 | .2 Subject area |        |        |            | Math                  | Mathematics                                     |            |      |     |                  |       |
| 2.3 | Course respons  | ible/l | ectur  | er         | Prof. dr. Dorian POPA |                                                 |            |      |     |                  |       |
| 2.4 | Teachers in cha | arge o | of app | olications |                       | Sl. dr. Alina RAMONA BAIAS                      |            |      |     |                  |       |
| 2.5 | Year of study   | Ι      | 2.6    | Semester   | 1                     | 2.7                                             | Assessment | exam | 2.8 | Subject category | DF/OB |
|     |                 |        |        |            |                       |                                                 |            |      |     |                  |       |

# 3. Estimated total time

| 3.1                                                                              | Number of hours per week                    | 4          | 3.2 | of which, course | 2  | 3.3 | applications | 2     |
|----------------------------------------------------------------------------------|---------------------------------------------|------------|-----|------------------|----|-----|--------------|-------|
| 3.4                                                                              | Total hours in the teaching plan            | 104        | 3.5 | of which, course | 28 | 3.6 | applications | 28    |
| Individual study                                                                 |                                             |            |     |                  |    |     |              | Hours |
| Manu                                                                             | al, lecture material and notes, bibliograph | hy         |     |                  |    |     |              | 20    |
| Supp                                                                             | lementary study in the library, online and  | in the fie | ld  |                  |    |     |              | 4     |
| Preparation for seminars/laboratory works, homework, reports, portfolios, essays |                                             |            |     |                  |    | 21  |              |       |
| Tutoring                                                                         |                                             |            |     |                  |    |     | 0            |       |
| Exams and tests                                                                  |                                             |            |     |                  |    | 3   |              |       |
| Other activities                                                                 |                                             |            |     |                  |    | 0   |              |       |
| 3.7                                                                              | 3.7 Total hours of individual study 48      |            |     |                  |    |     |              |       |
| 3.8                                                                              | Total hours per semester                    |            | 104 |                  |    |     |              |       |
| 3.9                                                                              | Number of credit points                     |            | 4   |                  |    |     |              |       |

#### 4. Pre-requisites (where appropriate)

| 4.1 | Curriculum | Basic knowledge of Differential Calculus and Set Theory                  |  |  |  |  |
|-----|------------|--------------------------------------------------------------------------|--|--|--|--|
| 4.2 | Competence | Competences in elementary Differential Calculus: elements of set theory, |  |  |  |  |
|     |            | limits, sequences and series, derivatives.                               |  |  |  |  |

| 5. Requirements (where appropriate) |                      |  |  |  |
|-------------------------------------|----------------------|--|--|--|
| 5.1                                 | For the course       |  |  |  |
| 5.2                                 | For the applications |  |  |  |

# 6. Specific competences

|            | C1 – Operating with basic Mathematical, Engineering and Computer Science concepts                                    |
|------------|----------------------------------------------------------------------------------------------------------------------|
|            | C1.1 – Recognizing and describing concepts that are specific to the fields of calculability, complexity, programming |
| nal<br>ces | paradigms, and modeling computational and communication systems                                                      |
| en         | <b>C1.3</b> – Building models for various components of computing systems                                            |
| ess        | C1.5 – Providing a theoretical background for the characteristics of the designed systems                            |
| ofo        |                                                                                                                      |
| Pr<br>CO   |                                                                                                                      |
|            |                                                                                                                      |
|            |                                                                                                                      |

| ses  | N/A |  |  |
|------|-----|--|--|
| ross |     |  |  |
| comp |     |  |  |
|      |     |  |  |

# 7. Discipline objectives (as results from the key competences gained)

| 7.1 | General objective   | A presentation of the concepts, notions, methods and fundamental techniques used in differential calculus.                                                                               |
|-----|---------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 7.2 | Specific objectives | Use of the differential calculus in order to solve problems in engineering.<br>Use of the differential calculus in modelling and solving practical problems<br>concerning spatial forms. |

# 8. Contents

| 8.1. L | ecture (syllabus)                                                                    | Teaching methods | Notes |
|--------|--------------------------------------------------------------------------------------|------------------|-------|
| 1      | Real numbers. Sequences of real numbers.                                             | Explanation      |       |
| 2      | Series of real numbers. Definition, examples and properties.                         |                  |       |
| 3      | Tests of convergence for series of numbers                                           | Demonstration    |       |
| 4      | Sequences of functions. Series of functions.                                         |                  |       |
| 5      | Power series. Taylor formula and Taylor series.                                      | Collaboration    |       |
| 6      | Trigonometric series. Fourier series.                                                |                  |       |
| 7-8    | Metric spaces. Topology of a metric space. Banach fixed point theory.                | Interactive      |       |
| 9.     | Functions of several variables. Limit and continuity.                                | activities       |       |
| 10-    | Differential Calculus for Functions of Several Variables. Partial derivatives.       |                  |       |
| 11     | Differential operators. Directional derivative. Differential of functions of several |                  |       |
|        | variables. Taylor's formula for functions of several variables.                      |                  |       |
| 12     | Extrema for functions of several variables.                                          |                  |       |
| 13     | Implicit functions.                                                                  |                  |       |
| 14.    | Conditional extrema.                                                                 |                  |       |
| Biblio | ography                                                                              |                  |       |
|        | 1. Dorian Popa, Calculus – Mediamira Cluj-Napoca, 2006.                              |                  |       |
|        | 2. O. Stănășilă, Analiză matematică, EDP București, 1981                             |                  |       |
|        | 3. Dumitru Mircea Ivan. Calculus. Editura Mediamira, Cluj-Napoca, 2002.              | - 1              |       |
| 8.2.   | Applications (Seminars)                                                              | Teaching methods | Notes |
| 1      | Exercises related to sequences of numbers.                                           |                  |       |
| 2      | Exercises related to series                                                          |                  |       |
| 3      | Exercices related to the convergence of series.                                      |                  |       |
| 4      | Exercises related to power series: convergence and evaluation of sum.                | Explanation      |       |
| 5      | Exercises concerning Taylor series.                                                  | _                |       |
| 6      | Exercises related to Fourier series                                                  | Demonstration    |       |
| 7      | Exercises concerning metric spaces and Banach Fixed Point Theorem.                   |                  |       |
| 8-     | Exercises related to: partial derivatives, derivative of composite functions,        | Collaboration    |       |
| 10     | gradient, directional derivative, differential of functions of several variables,    |                  |       |
|        | Taylor's formula for functions of several variables.                                 | Interactive      |       |
| 11-    | Exercises related to extrema for functions of several variables.                     | activities       |       |
| 12     |                                                                                      |                  |       |
| 13     | Exercises related to implicit functions, change of coordinates and variables.        |                  |       |
| 14     | Exercises concerning conditional extrema.                                            |                  |       |
| Bibli  | ography                                                                              |                  |       |
| 1.     | N Vornicescu, D.M.Ivan, D. Pona, Calcul diferential, Editura Mediamira, 2004         |                  |       |
|        | t. vonneesea, D.M.Ivan, D. Popa, Calcar anterengia, Eartara Medianna, 2001.          |                  |       |

# 9. Bridging course contents with the expectations of the representatives of the community, professional associations and employers in the field

Collaboration with engineers in order to identify and solve problems raised by the market.

| Activity type                                                                                     | 10.1                                 | Assessment criteria               | 10.2 | Assessment methods  | 10.3 | Weight in the final grade |  |
|---------------------------------------------------------------------------------------------------|--------------------------------------|-----------------------------------|------|---------------------|------|---------------------------|--|
| Course                                                                                            |                                      | Abilities of understanding and    |      | Written examination |      | 30%                       |  |
|                                                                                                   |                                      | using creatively the concepts and |      |                     |      |                           |  |
|                                                                                                   |                                      | proofs                            |      |                     |      |                           |  |
| Applications                                                                                      |                                      | Abilities of solving problems and |      | Written examination |      | 70%                       |  |
|                                                                                                   |                                      | applying algorithms               |      |                     |      |                           |  |
| 10.4 Minimum                                                                                      | 10.4 Minimum standard of performance |                                   |      |                     |      |                           |  |
| Ability to present coherently a theoretical subject and to solve problems with practical content. |                                      |                                   |      |                     |      |                           |  |
|                                                                                                   |                                      |                                   |      |                     |      |                           |  |

| Date of filling in: |              | Title NAME                 | Signature |
|---------------------|--------------|----------------------------|-----------|
| 13.09.2022          | Course       | Prof. Dorian POPA          |           |
|                     | Applications | SL. dr. Alina-Ramona BAIAS |           |

Date of approval by the Department Board 15.09.2022

Date of approval by the Faculty Council

Head of Department of MATHEMATICS Prof.dr. Dorian POPA

Dean Prof.dr.ing. Liviu Cristian MICLEA